A Brief History

Black Hole [definition]:

A region of space from which nothing, not even light, can escape.

When did the concept of a black hole originate? Earlier than you think.

Rev John Michell (1783) – “If [the size of] a sphere of the same density of the Sun were to exceed that of the Sun in the proportion of 500 to 1 ... all light emitted from such a body would be made to return towards it by its gravity.”

In the 1800s the idea of such 'dark stars' was largely ignored.
Warping Space and Time

A Brief History

Einstein (1915) General Theory of Relativity
Schwarzschild (1916) Calculation of gravity of a compact mass

Eddington (1926) Stars compressed to the 'Schwarzschild radius'
Chandrasekhar (1931) Massive stars at the end of their lives will collapse

Oppenheimer (1939) Nothing can stop the collapse of massive stars

General Relativity predicts that time stops at the Schwarzschild radius and so such collapsed stars were called 'frozen stars'.

Finkelstein (1958) At the Schwarzschild radius there is an event horizon – a 'one-way membrane'
Golden Age of GR and BH (~ 1960 – 1975) Kerr / Newman / Penrose / Hawking
1964 First use of the term 'black hole'
1967 Discovery of pulsars
1969 Identified as neutron stars
Gravitational collapse of stars is not just a hypothetical possibility!

Pieces of the Puzzle

Escape Velocity
General Relativity

Stars and Galaxies
Detecting Gravity

We will look at each of these pieces of the puzzle in turn
**Warping Space and Time**

**Escape Velocity**

What goes up must come down? Right?
Wrong, not if it goes up fast enough.

The threshold speed needed for an object to escape the gravitational pull of a body is called the escape velocity. If you throw something up with a speed less than the escape velocity then it will fall back.

The force of gravity pulling an object (like you) towards a body (like the Earth) depends on both of the masses involved and the distance between them. The escape velocity does not depend on the mass of the object — the escape velocity for a 1 kg satellite is the same as for a 1 ton satellite or even a 1000 ton space station.

**Escape Velocity**

The escape velocity at the surface of a body depends on the ratio of the mass to the radius \( M/R \).

Some escape velocities:

- Velocity to escape the Moon = 2 km/s \( (= 5,000 \text{ mph}) \)
- Velocity to escape the Earth = 11 km/s \( (= 25,000 \text{ mph}) \)
- Velocity to escape the Sun = 600 km/s \( (> 1,000,000 \text{ mph}) \)

600 km/s may sound like a lot, but it is only 0.2% of the speed of light.

**Escape Velocity**

Let’s compress the Sun to smaller sizes and see what happens to the escape velocity.

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**Escape Velocity**

If we compress the Sun into a sphere of radius 3 km then we form a black hole.

What if we start with a body with a different mass?

For the Earth the Schwarzschild radius is \(~ cm\)
- Moon \(~ 0.1 \text{ mm}\)
- Mt Everest \(~ \text{ atom}\)

We know of no way that this can happen for any mass smaller than that of a star, but that doesn’t mean that it’s impossible.
Warping Space and Time

Escape Velocity

Although all sizes are possible, small BH don’t last.

Aside: Quantum Mechanics* allows particles and antiparticles to be created from borrowed energy, as long as they annihilate and pay back the borrowed energy on very short time scales.

Escape Velocity

Although all sizes are possible, small BH don’t last.

How is this particle-antiparticle creation relevant to the lifetime of BH? What might happen if they are created just outside the event horizon?

There is a net flux of particles radiating from the event horizon of the BH called Hawking radiation. This radiation increases with decreasing mass, so small BH evaporate! More about this later in the talk.

Escape Velocity

What happens if we compress an object to a size smaller than the Schwarzschild radius?

The event horizon, the point at which the escape velocity is equal to the speed of light, is still the same (the Schwarzschild radius).

For massive stars (M > 10M_☉) nothing that we know of can stop the core collapse during a supernova and so all the mass is compressed to an infinitely small point – a singularity.

We cannot tell if this is what actually happens inside a BH because it is all hidden inside the event horizon. Could we ever see a “naked” singularity? Not according to the Cosmic Censorship Hypothesis.

General Relativity

Dr Steve Barrett

SCAS 20 Sep 2018
Warping Space and Time

**General Relativity**

Einstein's General Theory of Relativity  
First presented in 1915 and published in 1916

**What does it say?**

\[ G = 8\pi T \]

The main principle of GR can be expressed by this one equation that looks deceptively simple.

- **G** is the geometry of space
- **T** is the distribution of mass

Mass distorts space!

**General Relativity**

\[ G = 8\pi T \]

The equation is sometimes reduced to the more prosaic description

- **Mass** tells space how to curve
- **Space** tells mass how to move

**What do we mean by curved space?**

Any image trying to explain this uses the analogy of 2-dimensional space curving into a third dimension.

To warp or curve 3-dimensional space we need a fourth dimension which humans, not unnaturally, find very difficult to imagine.

**General Relativity**

Black holes produce infinitely warped space

**Predictions of General Relativity**

The precession of the orbit of Mercury

Gravitational lensing

Stars seen during the total solar eclipse of 1919 were found to be slightly shifted in position.
Warping Space and Time

**Predictions of General Relativity**

Time slows down in a gravitational field

**Gravitational Waves**

One of the predictions of GR is gravitational waves.

The ripples in spacetime are tiny — 1 part in $10^{20}$

**Gravitational Waves**

Merger of two neutron stars

**Gravitational Waves**

If binary pulsars emit gravitational waves they must be slowly losing energy, and this would mean that they would be expected to slow down (black line).

This is precisely what is observed (blue points).
Warping Space and Time

Stars and Galaxies

Black Holes Are Born
Core collapse of a massive star – Supernova*

Black Holes Feed
Infalling matter forms an accretion disk

Black Holes Feed
Accretion disk and x-ray jets

* See “The ABC of Stellar Evolution”
Warping Space and Time

Black Holes Feed
Accretion disk and x-ray jets
The infalling matter is heated by the tidal forces and emits light and x-rays. The accretion process can convert more than 25% of the infalling mass into energy. Compare this to nuclear fusion in stars, where less than 1% of the mass is converted into energy.

Black Holes Feed
Is this how black holes feed on neighbouring stars?

Black Hole Jets

Supermassive Black Holes
Zooming in to the centre of the Milky Way
Warping Space and Time

**Supermassive Black Holes**

**Stars orbiting the BH at the centre of the Milky Way**

- **How big is the SMBH at the centre of the Milky Way?**
  - From the orbits of the stars the SMBH mass is determined to be 4 million $M_\odot$.
  - Other SMBH are much larger:
    - Andromeda Galaxy: 250 million $M_\odot$
    - Sombrero Galaxy: 1 billion $M_\odot$
    - Largest SMBH: > 20 billion $M_\odot$

**Measuring Curved Space**

- **Gravity Probe B**
  - 2004

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Detecting Gravity
Warping Space and Time

Detecting Extreme Gravity

SWIFT
Gamma-Ray Burst Mission
2004

FERMI
Gamma-Ray Space Telescope
2008

Detecting Gravity Waves

LIGO
Laser Interferometer Gravitational Wave Observatory

The gamma-ray cycle of PG 1553+113

Detecting Extreme Gravity

Detecting Gravity Waves
Warping Space and Time

Detecting Gravity Waves

LIGO is sensitive to waves with periods of less than a second. This means that it can detect waves created by the merger of two black holes, but this does not happen very often.

By comparison, eLISA will be sensitive to waves with much longer periods, from seconds to hours. This should mean that eLISA can detect signals from BH within our galaxy and SMBH in other galaxies.

It is also hoped that eLISA will be able to detect the gravitational waves created by the biggest singularity of them all – the Big Bang.

* See "The Beginning of Everything"
Warping Space and Time

Measuring an Event Horizon

Event Horizon Telescope

Pieces of the Puzzle

Escape Velocity
General Relativity
We have looked at the science facts
Now let’s look at the science fiction
Stars and Galaxies
Detecting Gravity

Science Fiction

Does Hollywood ever get it right?

Ship is parked right next to the event horizon
Ship is pulled in to a planetary black hole
Ship is powered by an onboard black hole

Science Fiction

Is a BH-powered star drive possible?
For BH with mass less than a kg, not much energy is available (E = mc²).
For BH with a mass more than that of Mount Everest, Hawking radiation is very weak.
For BH with mass ~ 1 million tons the power in the Hawking radiation would be equivalent to the output of ~ 100 million nuclear power stations and the BH would last ~ 100 years.

If the radiation from such a BH, smaller than an atom, could be captured or directed, then that is enough energy to power a starship.
Warping Space and Time

**Science Fiction**

What about shortcuts through space?
Wormholes?
Hyperspace?

**Science Fiction**

What about shortcuts through space?
Wormholes?
Hyperspace?

**Science Fiction**

What about time travel?

**Science Fiction**

Hawking proposed the
*Chronology Protection Conjecture*

A wormhole allowing time travel will collapse before anything has time to travel through it.

"Making the Universe safe for historians"
Warping Space and Time

The Problem

There’s a problem.

General Relativity (GR) works really well for massive objects (like stars).
Quantum Mechanics (QM) works really well for tiny objects (like atoms).*

But, what if the object is massive and tiny? Then we need (drum roll)... Quantum Gravity.

The problem: GR and QM are not good bedfellows. A universal 'Theory of Everything' has proven to be elusive.

* See "The Weird World of the Very Very Small"

The Future

Maybe quantum mechanics will prevent a singularity from forming, thus avoiding the horrible properties like infinite density and infinitely warped space. For instance, String Theory describes a ten-dimensional universe in which the fundamental building blocks are 'strings' rather than the more familiar 'particles'.

If String Theory is right, black holes are 'fuzzballs' without a singularity at their core. They are just 'balls of string'. But, is the universe described by String Theory the one in which we live?

Einstein never really believed that quantum mechanics was the right description of the microscopic world.
He spent most of his later years wrestling with a Theory of Everything.
If a genius like Einstein could not get his head around the problem, what will it take?

Maybe some unexpected discoveries, for instance from LIGO or eLISA, will point the way forward to a better understanding of black holes.