## Formula for the Centroid of R

The area is

$$A = \int \int_{R} dx dy = \int \int_{R} dy dx.$$

The centroid is the centre of mass if mass on R is uniformly distributed. The formula for the centroid is

 $(\overline{x}, \overline{y}),$ 

where

$$\overline{x} = \frac{1}{A} \int \int_{R} x dx dy = \frac{1}{A} \int \int_{R} x dy dx,$$

and

$$\overline{y} = \frac{1}{A} \int \int_R y dx dy = \frac{1}{A} \int \int_R y dy dx.$$

Formula for the centre of mass with density  $\rho(x,y)$ .

If the mass has density  $\rho(x, y)$ , the weight of R is

$$W=\int\int_{R}\rho(x,y)dxdy=\int\int_{R}\rho(x,y)dydx.$$

The formula for the centre of mass is

$$(\overline{x}, \overline{y}),$$

where

$$\overline{x} = \frac{1}{W} \int \int_{R} x \rho(x, y) dx dy = \frac{1}{W} \int \int_{R} x \rho(x, y) dy dx,$$

and

$$\overline{y} = \frac{1}{W} \int \int_{R} y \rho(x,y) dx dy = \frac{1}{W} \int \int_{R} y \rho(x,y) dy dx.$$