

# Number of jumps in two-sided first-exit problems for a compound Poisson process

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## Abstract

In this paper, we study the joint Laplace transform and probability generating functions of two pairs of random variables: (1) the two-sided first-exit time and the number of claims by this time; (2) the two-sided up-crossing time and its associated number of claims. The joint transforms are expressed in terms of a generalized scale function. We also find explicit expressions for the joint density function of the two-sided first-exit time and the number of claims by this time. Numerical examples are presented for exponential claims.

**Keywords:** Classical risk model; Two-sided first-exit time; Two-sided up-crossing time; Number of claims; Generalized scale function

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